

# Risk Analysis of Highly-integrated Systems

VA: Vulnerability and Resilience



## Concept of vulnerability (Verletzbarkeit) – definition of terms (I)

- Disasters in the past revealed that “hazard-centric” perception / concepts are too limited as “a hazard of low intensity could have severe consequences, while a hazard of high intensity could have negligible consequences. The level of vulnerability was making the difference“ (White, 1974).
- Hazard = Gefahr (threat = Gefahr, Bedrohung): ... a possible / potential source of danger....

## Properties and characteristics of hazards

Hazard's characteristics	Description
Nature	Natural, socio-natural, technological, sociopolitical, man-made hazards
Magnitude	Only those occurrences that exceed some common level of magnitude are extreme
Location or geographical extent	Space covered by the hazardous event
Spatial dispersion	Pattern of distribution over the space in which its impact can occur
Speed of onset	Length of time between the first appearance of an event and its peak
Duration	Length of time over which a hazardous event persist, the onset to peak period
Frequency/Probability	The sequencing of events, ranging along a continuum from random to periodic. From the frequency the probability of return can be defined

Source: S. Bouchon, after Gravley, 2001

## Concept of vulnerability – definition of terms (II)

### No consensus definition of vulnerability to date

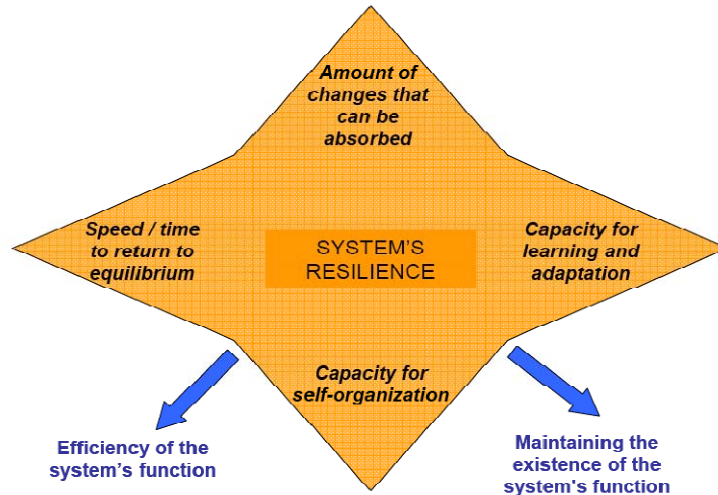
We define **vulnerability** as a flaw or weakness (inherent characteristics including resilience capacity) in the design, implementation, operation and/or management of an infrastructure system or its element to a hazard or threat.

The concept of vulnerability develops in three main steps and finally focuses on three elements:

- Degree of loss and damages due to the impact of a hazard (technical dimensions),
- Degree of exposure to the hazard, i.e. likelihood of being exposed to hazards of a certain degree and the susceptibility of an element at risk to suffer loss and damages (element at risk could be a technical system),
- Degree of capacity of resilience, i.e. the ability of a system to anticipate, cope with/absorb, resist and recover the impact of a hazard (technical) or disaster (social)

Resilience: ability to recover from some shock or disturbance – the quality or state of being flexible.

## Features of system's resilience



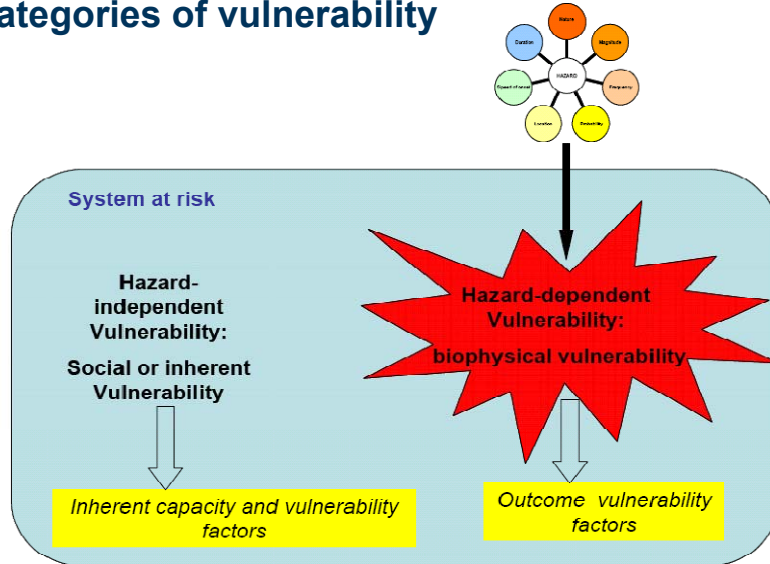
Source: S. Bouchon

## Concept of vulnerability – definition of terms (III)

Distinction between two categories viewing vulnerability either

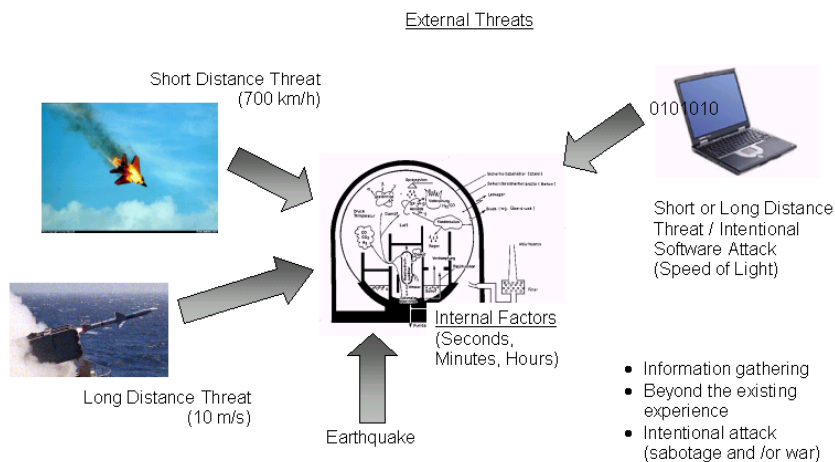
1. as the amount of (potential) damages caused to a system by a particular hazardous event (hazard dependent, biophysical vulnerability)
2. as a state that exists within a system before it encounters a particular hazardous event (hazard independent, inherent vulnerability)

## Categories of vulnerability



Source: S. Bouchon

## Vulnerability-Technical Example

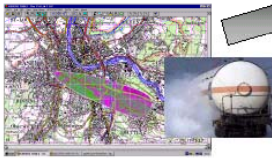


## Vulnerability-Societal Example

Intentional Attack (Cargo Airplane)



External Threats



Accidental Situation  
(Transportation Dangerous Goods)



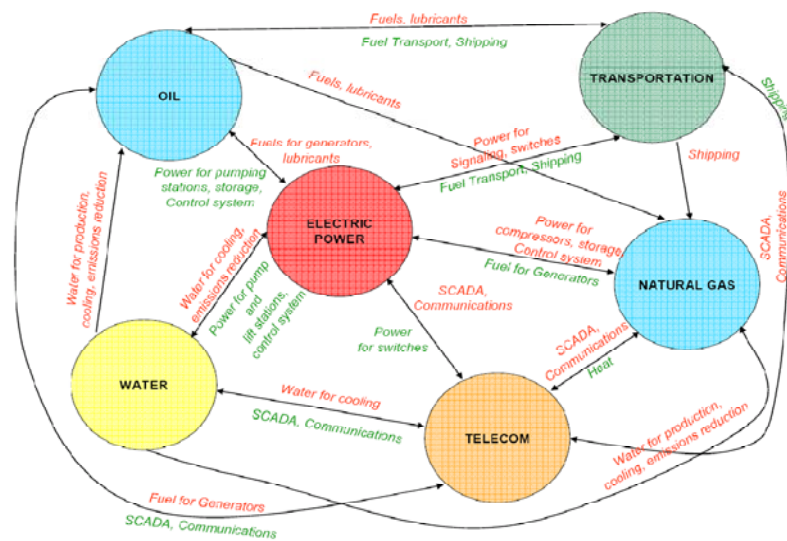
Congested  
and/or crowded  
areas

Internal Factors

- Technical Failure
- Panic
- Un-managed police intervention
- Weak management of the establishment

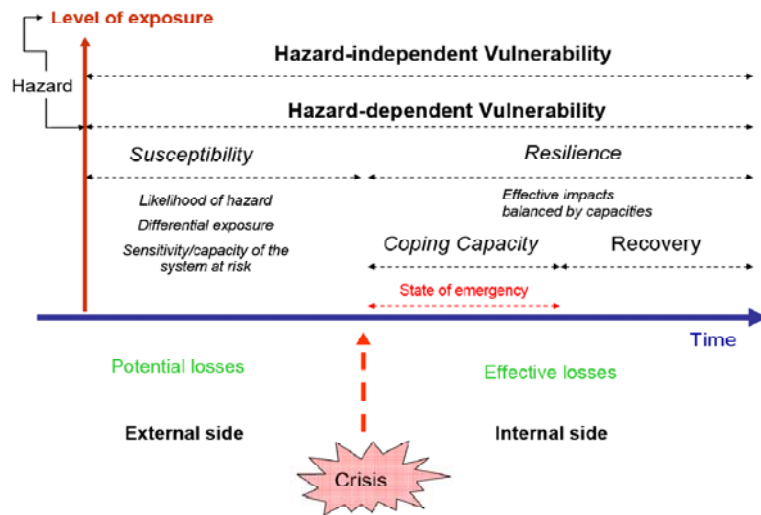
Vulnerability Assessment

## Critical infrastructures and their interdependencies



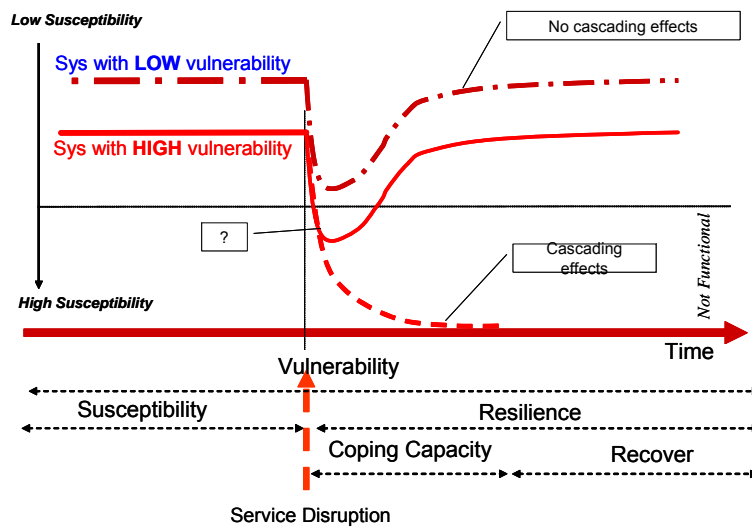
Source: Rinaldi, Peerenboom, Kelly, 2001

## Vulnerability model



Source: S. Bouchon

## Vulnerability scenarios



## Vulnerability Assessment of Networks Examples of technical networks

Swiss Power System



Natural Gas Pipelines



- Internet
- World Wide Web
- Railway
- Motorway
- ...

## Multicomponents System's Vulnerability – Representation by U, V, t, modeling approach

### System

- consists of large number,  $M$ , of elemental constituents, or members

### System members

- interact with each other with a varying intensity; interaction described by a coupling constant, or intrinsic parameter  $U$ , and an exterior factor, or extrinsic parameter  $V$ .
- may assume two distinct states, 1 and 2, normal vs. abnormal, up vs. down, etc., at given time,  $t$

### Overall state of the system

- described via a pair of numbers  $(M_1, M_2)$ , system dynamics, or motion in its space will follow from variations in  $M_1$  and  $M_2$ .



## Multicomponents System's Vulnerability (I)

Smallest transitions in the system's state involve alterations by one unit in the numbers of members:

$$(M_1 - 1, M_2 + 1) \xleftarrow{w_{12}} (M_1, M_2) \xrightarrow{w_{21}} (M_1 + 1, M_2 - 1) \quad (1)$$

while  $w_{12}$  and  $w_{21}$  are governing probabilities.

Admission of the process leads also to the recognition of a function of distribution of the system's states:

$$\begin{aligned} \partial f(M_1, M_2, t) / \partial t = & w_{21}(M_1 - 1, M_2 + 1) \cdot f(M_1 - 1, M_2 + 1) + \\ & + w_{12}(M_1 + 1, M_2 - 1) \cdot f(M_1 + 1, M_2 - 1) - \\ & - (w_{21}(M_1, M_2) + w_{12}(M_1, M_2)) \cdot f(M_1, M_2) \end{aligned} \quad (2)$$

## Multicomponents System's Vulnerability (II)

The state (M1, M2) of the system can alternatively be described by the membership fraction

$$\zeta = (M_1 - M_2) / (2M), \quad (3)$$

if all system members are in state 1, then  $\zeta = 1/2$ , whereas if all members are in state 2, then  $\zeta = -1/2$ .

Equation (2) may be re-written as:

$$\begin{aligned} \partial f(\zeta) / \partial t = & w_{21} (\zeta - 1/M) f(\zeta - 1/M) + w_{21} (\zeta + 1/M) f(\zeta + 1/M) - \\ & - (w_{21} (\zeta) + w_{12} (\zeta)) f(\zeta) \end{aligned} \quad (4)$$



## Multicomponents System's Vulnerability (III)

Transition probabilities  $w_{12}$  and  $w_{21}$  need to assumed, e.g. if transitions are a co-operative phenomenon

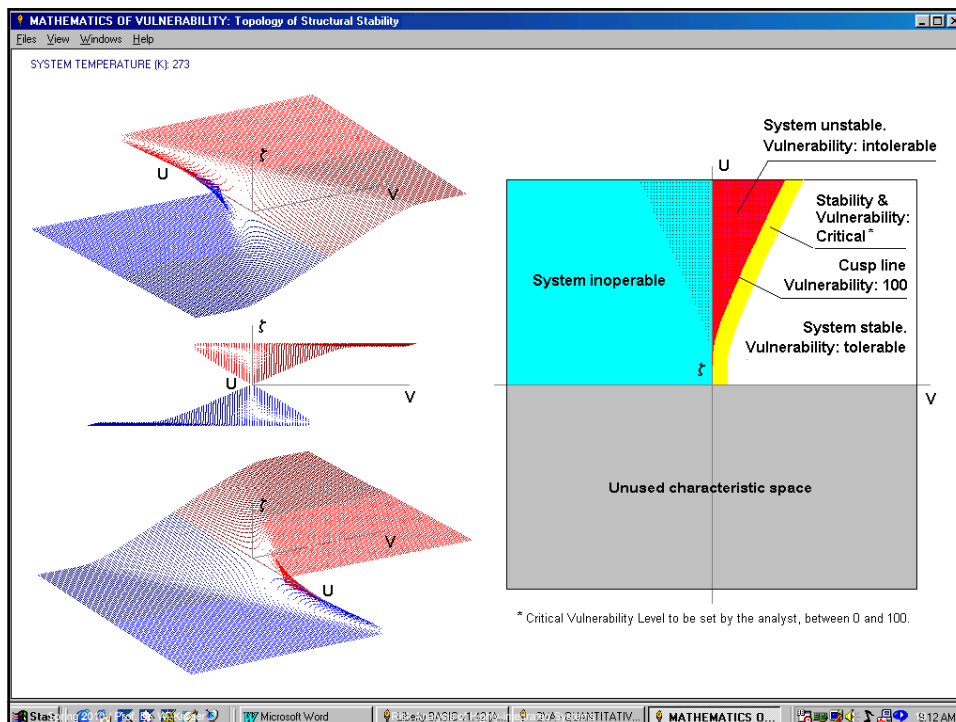
$$\begin{aligned} w_{12}(\zeta) &= w \cdot M_1 \cdot \exp(-U \cdot \zeta + V) / \theta \\ w_{21}(\zeta) &= w \cdot M_2 \cdot \exp(U \cdot \zeta + V) / \theta \end{aligned} \quad (5)$$

$\theta$  generalised 'temperature' of the system

## Real solutions $\zeta$

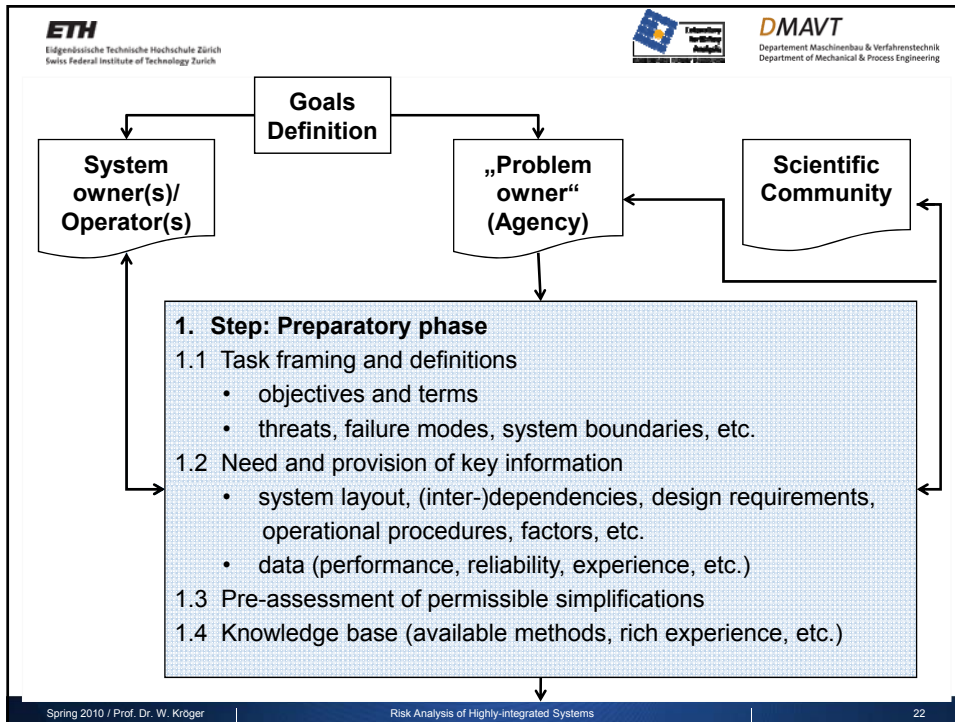
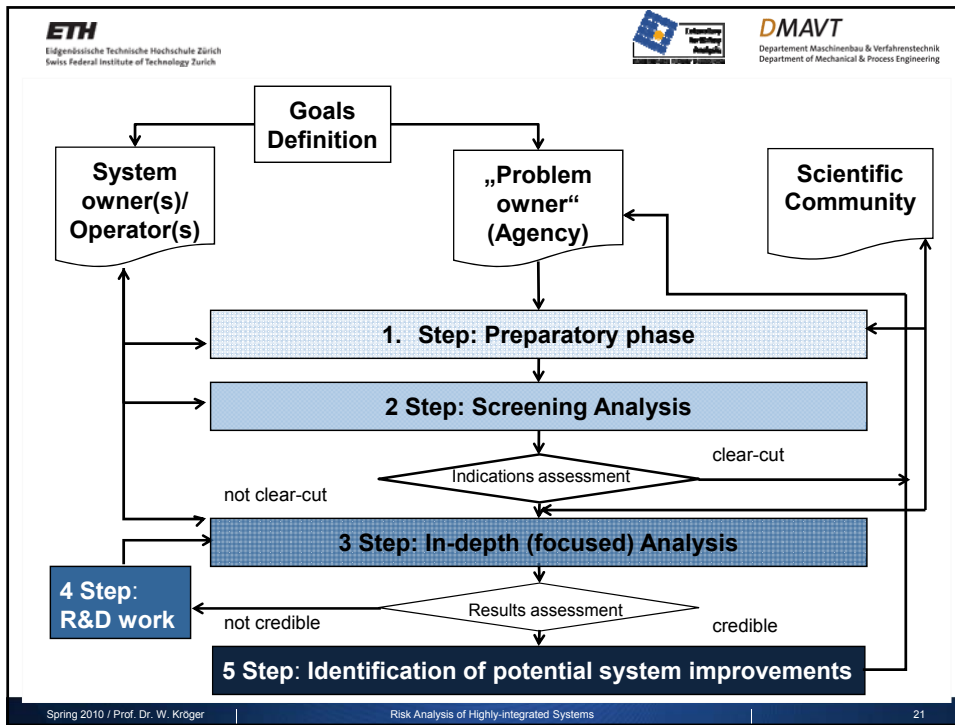
Depending on the degree of interaction between system constituents (members), reflected in the coupling constant  $U$ , and on the external influence on all system members - reflected in the field  $V$ , and also taking into consideration the temperature  $\theta$  of the system, the equation may display the following number of real solutions  $\zeta$  that may relate to the overall system condition:

Number of Real Solutions	System Condition
1	Stable. Smooth transitions in population membership, between state 1 and state. <b>Low and/or acceptable vulnerability.</b>
3, of which 2 identical	Critical. Sharp transitions in membership between states 1 and 2 are possible. Either state 1 or state 2 may suddenly become improbable. <b>System is critically vulnerable.</b>
3, all different from each other	Unstable. Sharp transitions in membership between states 1 and 2 are possible. Frequency of occurrence of states 1 and 2 are comparable. <b>System is dangerously/ un-acceptably vulnerable.</b>



## Motivation

- **Requirements:** Vulnerability analysis of interconnected infrastructures calls for 'system-of-systems thinking', suitable techniques and problem-oriented approach.
- **Available:** Many models for analyzing individual critical infrastructures
- **Missing:** Comprehensive framework for modeling and simulation of interdependencies



## Threats to Electric Power Supply Infrastructure

